

**ALGEBRA EXAMPLE 1**

The function  $f$  defined by  $f(x) = -x^2 + 6x - 5$  has

- (A) A minimum  $y$  value and a negative  $y$ -intercept.
- (B) A maximum  $y$  value and a positive  $y$ -intercept.
- (C) A minimum  $y$  value and a positive  $y$ -intercept.
- (D) A maximum  $y$  value and a negative  $y$ -intercept.

**SOLUTION**

$$f(x) = -x^2 + 6x - 5$$

Look at the  $x^2$  term. It is negative, so the graph will look like this:  
This means that the function has a maximum value.



The intercept occurs where  $x = 0$ .

$$\therefore f(0) = -(0)^2 + 6(0) - 5 = -5$$

This means that the  $y$ -intercept is negative.

Now we know that the function has a maximum  $y$  value and a negative  $y$ -intercept.

Compare this with options (A), (B), (C) and (D).

The correct answer is D.