

NUMBER PATTERNS 6: QUIZ SOLUTIONS

Question 1

What is the sum of an arithmetic series with 10 terms whose first term is a and common difference d ?

- A. $S_{10} = 5(2a + 9d)$ B. $S_{10} = 5(a + 9d)$ C. $S_{10} = 10(2a + 10d)$
D. $S_{10} = 10(a + 10d)$

Solutions

$$\begin{aligned} S_{10} &= \frac{1}{2} \times 10[2a + (10 - 1)d] \\ &= 5(2a + 9d) \end{aligned}$$

So, the correct answer is A

Question 2

An arithmetic series with 12 terms is $a + b + c + \dots + k$. What is the sum of the series?

- A. $S_{12} = 6(2a + 11k)$ B. $S_{12} = 6(a + k)$ C. $S_{12} = 12(a + k)$
D. $S_{12} = 12(2a + 11k)$

Solution

$$S_{12} = \frac{1}{2} \times 12(a + k) = 6(a + k)$$

So, the correct answer is B.

Question 3

What is the sum of the arithmetic series $1 + 2 + 3 + \dots + k$?

- A. $\frac{1}{2}n(n + 1)$ B. $\sum_{k=1}^n k$ C. $\sum_{r=1}^n r$ D. $\frac{1}{2}k(k + 1)$

Solutions

$$S_n = \frac{1}{2} \times k[2(1) + (k - 1)(1)] = \frac{1}{2}k(k + 1)$$

So, the correct answer is D.

Question 4

An arithmetic series is $1 + 2 + 3 + \dots$. What is the sum of the 20th to 40th terms, inclusive?

- A. 590 B. 610 C. 630 D. 671

Solution

$$\begin{aligned}\text{Sum from } T_{20} \text{ to } T_{40}, \text{ inclusive} &= S_{40} - S_{19} \\ &= \frac{1}{2} \times 40[2(1) + (40 - 1)(1)] - \frac{1}{2} \times 19[2(1) + (19 - 1)(1)] \\ &= 20(41) - \frac{1}{2} \times 19(20) \\ &= 820 - 190 \\ &= 630\end{aligned}$$

So, the correct answer is C.

Question 5

What is the value of $\sum_{m=1}^k 1$?

- A. k B. m C. 1 D. $k + m$

Solution

$$\begin{aligned}\sum_{m=1}^k 1 &= 1 + 1 + 1 + \dots + 1 \\ &\quad \text{\color{red} } k \text{ terms} \\ &= k\end{aligned}$$

So, the correct answer is A.